Apple Stock Price Prediction: Final Report

[GitHub Link](https://github.com/saimoom026/Springboard/tree/student-branch/springboard/Capstone%20two)

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# Problem Statement

## Project Flow

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1. **Start with the business problem**

Apple’s stock price forecast is of great interest for millions of individual investors, stakeholders, suppliers, manufacturers. Accurate forecast can yield significant profit gain.

1. **Convert business problem into time-series forecasting problem**

Conventional models are good for short term forecast (~a year). They cannot consider holiday effects or any trend change (e.g. economic downturn) in history that needed attention in prediction modelling.

1. **Solve time-series forecasting problem**

FBProphet, an open source library of Facebook, can incorporate holiday effects on top of paying attention to the exceptional circumstances in terms of trend change model.

1. **Convert time-series forecasting solution into business solution**

Better accuracy can yield significant profit margin. Better long term accuracy can help financial planning of the company itself and the investors, stakeholders

## Business Understanding

Apple Inc. is one of American the big tech multinational technology companies, headquartered in California, that is known for the fine design, development and selling of consumer electronics, computer software and online services. It is one of the top 10 Fortune 500 companies and ranks top in the Nasdaq stock exchange. Its stock price is closely watched by millions of people around the world. Short, medium, and long-term stock prediction is of interest for investors, companies to plan their financial strategy well ahead of time. During the economic downturn stock market prediction becomes even more complex. Given the long historic data that captures rare economic downturn events can provide insight for better prediction coupled with relevant features (dividend, earning). This project will aim in that pursuit.

## Time-Series Forecasting

The primary objective is to come up with a better forecasting model for Apple’s Stock price prediction. The conventional models can consider for past couple of years. It is observed that, during, before or after holidays financial behavior changes and can have effect on the stock price. Also think of the economic recession in 2008 and sharp price fall in 2014. These types of sudden trend changes if incorporated into the forecasting model, can yield better forecasting model.

# Data Collection

## Data Source

Stock price data was collected from the [Kaggle website](https://www.kaggle.com/tsaustin/us-historical-stock-prices-with-earnings-data?select=stocks_latest) sourced from NASDAQ, Yahoo finance, Zacks, Alpha vintage. Data consisted of 700+ companies over the years of 1998 – 2020. Along with the stock price information, dividend and earning information came up with the data source.

## Getting to Know around the Data Set

The data package consisted of four files: dividend, earning, stock price and summary. The Dividend file consisted of the following columns:

|  |  |
| --- | --- |
| **Dividend** | |
| **symbol** | symbol of a company under which it operates in stock market |
| **date** | dividend issue date for a share |
| **dividend** | proportion of dividend issued |

The ‘earning’ file looks like:

|  |  |
| --- | --- |
| Earnings | |
| symbol | symbol of a company under which it operates in stock market |
| date | earning issue date |
| qtr | the month and quarter (Q1, Q2, Q3 and Q4) of the year the earning was declared |
| eps\_est | estimated eps (earning per share) |
| eps | exact eps |
| release\_time | earning issue date before or after the declaration date |

The ‘stock price’ file has the following columns:

|  |  |
| --- | --- |
| Stockprice | |
| symbol | symbol of a company under which it operates in stock market |
| date | trading day of the year |
| open | opening price in a day |
| high | high price for a day |
| low | low price in a day |
| close | closing price for a day |
| close\_adjusted | amended price that truly reflects stocks value after any corporate actions |
| volume | total volume traded in a day |
| split\_coefficient | the ratio by which a firms outstanding share increases following a stock split. Higher is the 'stock split' reduced the price would be |

The ‘summary’ file contains the summary of the other dataset, which will be picking up in the exploratory data analysis stage. Therefore, it will not be used for the project.

# Data Wrangling

Data wrangling consisted of cleaning up the data by removing NaN in the dataset and looking for duplicates.

## Removing NaN

NaN values were only found in ‘dividend’ dataframe. Looked closely, ‘eps’ got 21.5 % NaN which was seen missing during and after economic recession in 2008. Apart from the missing ‘eps’, ‘eps\_est’ have 21.4% missing values which were assigned with the ‘eps’ value that would be a close estimate of ‘eps’. The ‘release\_time’ had 28% missing value which were forward filled always in the history release time was declared after the eps announce date. The ‘qtr’ had 0.8 % missing value which information were filled from the date column

## Duplicates

No duplicated rows were found.

## Save Apple Specific Data

The dividend, earning and stockprice information were merged for only Apple and saved for exploratory data analysis (EDA).

[Jupyter Notebook for the Data Wrangling part can be found in this link.](https://github.com/saimoom026/Springboard/blob/student-branch/springboard/Capstone%20two/Stock-price-prediction-data-wrangling.ipynb)

# Exploratory Data Analysis

Time-series stock price data along with dividend and earning data can be very insightful in determining, daily, weekly, monthly, quarterly behavior of stock price. Correlation between variables will also be determined. Finally, only the variables relevant for forecast modelling will be saved.

## Seasonal Price Variation

### Day of the Week

Stock market is open on Weekdays only (Monday to Friday). Closing price was grouped by day of the week and taken 'median' over the years. Median was chosen over mean because, it will put more emphasis on regular prices and less on unusual time such an economic down turn's.

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In a week, Friday saw highest average closing price, whereas Wednesday saw the lowest.

### Month of the Year

Historically, it was determined which month of the year saw the largest closing price. Closing price was grouped by day of the week and taken 'median' over the years

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Month of May saw the highest closing price whereas December saw the lowest.

### Quarter of the Year

Determined which quarter of the year saw the largest closing price. Closing price was grouped by quarter of the year and taken 'median' over the years.

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Last quarter of the month saw the highest price followed by the start of the year.

## Stock Price Change

Stock price change (%) over a time duration is a good measure of how investment is growing.

### Month of the Year

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Apples share holders saw biggest return over the month of October and lowest return in June.

### Quarter of the Year

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Second quarter of the year saw the biggest return (%) followed by the Q4, whereas Q4 saw the highest quarterly rice shown earlier.

## Earning per Share (EPS) over the Quarters

EPS reflects how much revenue the company is generating with the share holder’s money.

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Apple showed best economic performance in the first quarter (Q1). Just after the Christmas big sale which makes sense.

## Traded Volume over Months

Traded volume data often overlooked while dealing with stock market analysis. Given the availability of time-series volume data, monthly variation of volume over years will be displayed.

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Highest traded month is September whereas lowest is July. Looking into the highest closing price month, it is May and lowest is in December. Apparently lowest price is associated with the highest trade volume and vice versa.

## Yearly Dividend Paid

Dividend are share of company's profit paid real to the customers. It is a real income which you can use to buy grocery, go for vacation, or invest back in the market. Higher the dividend better is the chance to increase demand and the share price.

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There is a dip noticed in 2014 also visible in sharp price drop during this time. Lately in 2018-2020, although there are increase in dividend but the raise from previous year have dropped.

## What happened in 2014?

There is a sharp closing price fall seen in 2014. Let's look closely what triggered the price fall. Apple's stock split happened three times in history, 2000, 2005 and 2014. When stock price crosses 100 $, the company can decide to for stock split to keep the price down to accommodate more investor. In 2014, Apple's [rice soar to 600 $. Just after the stock split by a ratio of 7, price stabilized under 100 $ seen from the following figure. Learn more about the Apple's stock slpit: <https://www.cnet.com/news/dont-freak-out-heres-why-apples-stock-is-below-100/>

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## Economic Recession in 2008

Economic recession in 2008 still fresh in the memory for many of us. Let's visualize how the stock's price evolved during that time. In the history, it is known as 'Great recession and officially existed between (December 2007 - June 2009). Link: <https://www.investopedia.com/articles/economics/08/past-recessions.asp>

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Clearly there is a break in the trend change during the recession time (shaded area).

## Anomalies and Outliers

Stock price is very unpredictable, and the data could have lots of variabilities. In determining 'Anomalies' boxplot for individual variables were plotted and amount of outliers was determined by inter quantile range (IQR).

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Anomalous data calculated is 19.58 (%). Which is quite significant and high possibility they are coming from the unpredictable stock price swing.

## Correlation between Variables

Based on Pearson's correlation coefficient, the variables will be grouped into high, moderate and low similarities (<https://www.statisticssolutions.com/pearsons-correlation%20coefficient/>). Here only the highly correlated variables will be displayed.

### Highly Correlated Variables

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From high to low correlation found between:

* prices (close, high, low, open) ----- dividend (0.80). This tells there is a high chance when price goes up, dividend goes up too and vice versa
* close adjusted ----- eps (0.72)
* close adjusted ----- dividend (0.61)
* eps ----- dividend (0.52)

## Feature Removal and Preparing for Modelling Stage

As the goal is to predict stock price based on historical data, only closing stock price data was saved. The low and moderate correlated features are needed when doing regression analysis

[Jupyter Notebook link for the EDA part can be accessed through this link.](https://github.com/saimoom026/Springboard/blob/student-branch/springboard/Capstone%20two/Stock-price-prediction-EDA.ipynb)

# Data Pre-processing

## Trend-Seasonality Decomposition

Investors always hope the prices would increase day by day. But price fluctuates over days and eventually see some gain over months, quarters, or years. Like any time-series data, stock price can be decomposed into trend, seasonality, and residual parts. This was done with ‘statsmodel’ library in Python.

* **Trend:** price tendency over a time. e.g. if the price is increasing/decreasing over a year
* **Seasonality:** periodic variation in the price that we see every year. It tells which part of the year price increases/decreases and that happens in cyclic manner over the years
* **Residual:** non-systematic component of the price which is not structured and termed as noise

A close up of a map

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The trend for Apples stock price is increasing for most of the time, there are few decreasing trends which come from stock splits and market adjustment. Seasonality is constant over time but follows strictly cyclic manner. That is every year there are specific times when stock rises and falls, and the pattern follows every year.

## Stationarity Check

A time-series is called stationary if the mean and standard deviation remains constant over time.

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Looking into the above figure, it is clear the mean and standard deviation is time varying and non-stationary. Before feeding the data for time series forecasting, the data needs to be tested for stationarity and transformed if required.

There is many testing for stationarity. Of the many, two mostly used stationarity checks will be done based on statistical hypothetical testing.

### ADF (Augmented Dickey-Fuller) test:

This method looks for unit root in the series. The hypothesis for this test is:

**Null Hypothesis:** The series has a unit root (value of a =1) (non-stationary)

**Alternate Hypothesis:** The series has no unit root (stationary)

If the p-value is less than 0.05 then we can reject the null hypothesis i.e. the data is stationary and the data has constant mean and variance over time.

### KPSS (Kwiatkowski–Phillips–Schmidt–Shin) test:

Slightly less popular than ADF, but needed as a double check along with ADF test. The hypothesis for KPSS test is opposite of ADF test:

**Null Hypothesis:** The process in trend stationary (non-stationary)

**Alternate Hypothesis:** The series has a unit root (stationary)

If the p-value is greater than 0.05 then we can reject the null hypothesis i.e. the data is stationary, and the data has constant mean and variance over time.

|  |  |  |
| --- | --- | --- |
|  |  |  |
| Stationarity test on the original time-series data | | |
| Method | p-value | Decision |
| ADF | 0.21 > 0.05 | Non-stationary |
| KPSS | 0.01 < 0.05 | Non-stationary |

Both tests confirmed non-stationarity of the original time-series stock data.

## Transform Data for Stationarity

Mainly two types of transformation can be applied:

**1. Differencing:** defined as, y(t) = y(t) - y(t-n). when n=1 then we are taking differences between two days (given daily data). like wise, if n=30, then taking changes for a month. differencing method is especially useful when the mean of the data is time varying

**2. Transformation:** generally applying logarithm. root or power transform to make the time varying variance stationary. Log is used to dampen out highly varying data. whereas power is used when the variance decays down over time.

For our case, we will start with differencing method as from the seasonality we observed varying mean over time.

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Time variation on the rolling mean and standard deviation have greatly reduced.

|  |  |  |
| --- | --- | --- |
|  |  |  |
| Stationarity test on the differenced time-series data | | |
| Method | p-value | Decision |
| ADF | 0.00 < 0.05 | Stationary |
| KPSS | 0.1 > 0.05 | Stationary |

Suggests the Apple daily price differenced data is stationary.

## Train-Test Split

Like any other analysis time series forecasting also requires, test data which will be used to test the integrity of the prediction. We have almost 20 years of stock price data. The training data will be taken from the 1998 till end of 2015. The rest of the data (2016-2020) will be used at test data.

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[Jupyter notebook for the pre-processing step can be found in this link.](https://github.com/saimoom026/Springboard/blob/student-branch/springboard/Capstone%20two/Stock-price-prediction-preprocess.ipynb)

# Machine Learning Modelling

## Auto Regressive Integrated Moving Average (ARIMA)

ARIMA model will be used which is one of the most used tools for forecasting time-series data and stands for Auto Regressive Integrated Moving Average. Generally, ARIMA model can be expressed as:

**predicted Y(t) = constant + linear combination lags of Y(t) (p lags) + linear combination lags of error in prediction terms (q lags)**

For example, Y(t) = 5 + 3 Y(t-1) + 2 𝜙(t-1).

Here, p=q=1. d stands for differencing needed for Y(t) to make the stationary.

There are many ways to determine best possible combinations of p, d and q values for a ARIMA model given a time series data. One way would be manually plotting auto correlation function (ACF) and partial autocorrelation function (PACF) for combinations of p, d and q parameters and determine the case for near zero ACF and PACF values. Here we will use auto\_arima function that will output best optimized model parameters for ranges of p, q values based on Akaike information criterion (AIC). AIC is an estimator which assess the statistical quality of a model. Model with a lower AIC value results in the best fit with the training data with least features.

The auto\_arima function can do the grid search over p, d, q (related to ARIMA model) and P, D and Q (related to seasonal components) parameters and report back the model with best AIC value.

### Finding Best Model Parameters

The auto\_arima function was applied on the time-series stock data and best p, d, q parameters were search by grid search method. Best ARIMA model order was found to be (p, d, q) = (0,1,0), with AIC = 46910.

Residual statistics from auto ARIMA model needs to be reviewed for integrity of the model. Residuals should be closer to noise like statistics, which confirms not containing any information from the data

A screenshot of a cell phone

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Couple of observations from the above residual plot:

* **Top left**: residual values seem to fluctuate around zero values and uniform variance except at the tail end. This is coming from the steep downing of the price after stock split in 2014
* **Top right**: The density plot suggests resemblances of residual distribution (orange color) with normal distribution (green one), with a mean zero
* **Bottom left**: The blue dots should perfectly align with the red line for a ideal scenario. This is the best possible alignment with the data
* **Bottom right**: The ACF of residuals are not correlated from the plot. Any correlation would suggest there are residual pattern in the data which is not explained in the model and needs parameter adjustment

Overall, it appears to be a good model and ready to use for forecasting.

### Forecast with ARIMA Model

Now take the best ARIMA model to predict the stock price and compare with the test data set.

A close up of a map

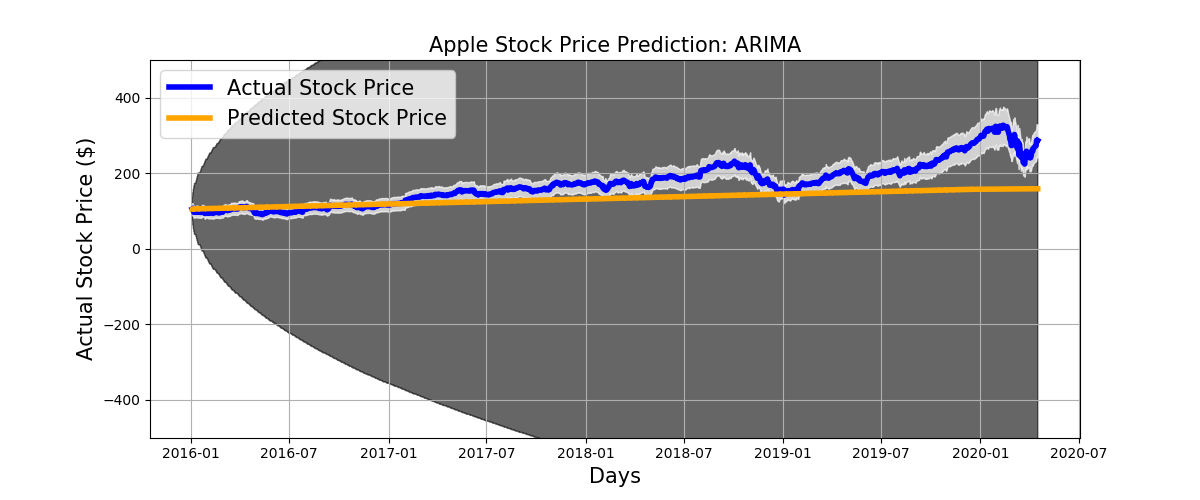
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Observations:

* The predicted stock price (in orange) seemed to follow the test data (blue) well initially. After that it deviated from the observed test data
* The shaded grey region is the 95% confidence interval. Over time the confidence interval widens up, meaning the model loses its capability to confidently predict price over time

### Look Closely into the Predicted Price

Prediction will be plotted only for 2016-2020 for better observations



Observations:

* The predicted price (orange) falls within the 15% price variation (white shaded region) over the 2016-2017
* Beyond 2017, predictions are in proximity with observed price and follow the trend but outside of 15% margin
* This suggests the built model can predict price well for a year
* Prediction line seems like a linear line, not following the randomness patterns of the stock price data

### Performance Measure

Commonly used accuracy measures for time-series forecasting models are mean squared error (MSE), mean absolute error (MAE), root mean squared error (RMSE), mean absolute percentage error (MAPE). We will be using these metrics on the forecast and test data to measure model performances.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| ARIMA | 2288.39 | 36.92 | 47.83 | 0.19 | 593.33 |

* Lower the metrics better the model would be
* We will compare this performance result with FBProphet model in the next part of the project

## FBProphet

Classic forecasting models such as ARIMA needs lots of parameter tuning and expert knowledge in statistics and analytics. Facebook developed an open source library called FBProphet, which requires truly little domain knowledge, easy to integrate in automated production environment. BBProphet decomposes any time series data into trend, seasonality, event, or holidays components and can be written as:

**Y(t) = T(t) + S(t) + H(t) + 𝜖**

**T(t):** piecewise linear or logistic growth curve for modelling trend components **S(t):** cyclic changes in the time-series (dily/weekly/monthly/quarterly) **H(t):** effect of holidays or unscheduled events **𝜖**: noisy term that can not be modelled with equation.

As opposed to time-based dependence, FBProphet considers forecasting as curve fitting problem.

In this section, FBProphet will be used to model Apple stock price prediction. Modelling will start with a base model, then adding main three aspects of FBProphet, saturating growth, trend change and holiday effect.

### Base Model

Let’s build first FBProphet model with Apple stock price data with 95% confidence level. The base model included the weekly, yearly seasonality.

#### Plot the Forecast

A close up of a map

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The ‘dark blue’ line is the observed data. The ‘light blue’ line is the forecast data. The shaded region is the 95% confidence area.

#### Look Closely on the Test Data

A close up of a map

Description automatically generated

The predicted price (orange) added randomness and following well with the randomness of the test data.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_base | 2277.77 | 35.64 | 47.72 | 0.19 | 590.33 |

The average\_score for FBProphet base model and ARIMA model are neck to neck.

### Saturation Forecast

Sometimes prior knowledge of the maximum and minimum possible of forecast values can be useful, in keeping the curve fitting on track. Here, we will add maximum stock price of 800 USD, which is a safe assumption, given stock split occurs usually at 100 USD closing price. Minimum price will be set at 0 USD.

#### Plot the Forecasting

A close up of a map

Description automatically generated

Looking into the predicted line (deep blue), frequent cycles appeared which does not follow much with the real data.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_saturating | 20332.25 | 129.26 | 142.59 | 0.71 | 5151.20 |

Considering saturating point, model performed worse than the base model which is reflected on the average\_score.

### Trend Changepoints

FBProphet automatically detects trend change points in the time-series. However, there are options for finer control if the expected trend change points are not captured with automatic control. It will be interesting to see, if FBProphet can capture major economic downturns happened in the past decades which might have impact on the forecasting.

#### Modelling

We figured out an important parameter for the prophet model is changepoint\_prior\_scale, which determines the trend flexibility in the model (default value is 0.05). Higher value leads to overfit (more flexible) and lower value leads to less flexible model. This best scale parameter was found measuring the lowest RMSE point over 0.01 and .02 ranges.

A close up of a map

Description automatically generated

Best scale for minimum RMSE score is 0.105. With this, trend change model will be trained and performance measured.

#### Plot the Forecasting

In FBProphet model, the time stamp column is denoted as ‘ds’ and the value column name is denoted by ‘y’.

A close up of a map

Description automatically generated

* Seeing the changepoints, the model is taking into account the trend changes during 2008 recession (middle stripped red lines)
* It is also including high number of trend changes visibly seen after 2012
* FBProphet automatically tracks trend changes and it is doing a good job for this scenario considering 2008 recession and 2014 sharp stock split. Trend change points can be manually set as well.

#### Look Closely on the Test Data

A close up of a map

Description automatically generated

Tuning up with trend change options, alignment between the observed (dark blue) and predicted (orange) data visibly improved a lot and persisted for most of the duration.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_trendchange | 1241.24 | 28.52 | 35.23 | 0.18 | 326.29 |

Considering trend change points yielded much better result than any other models and reflected with lowest average\_score so far.

### Seasonality

By default, FBProphet will fit weekly and yearly seasonality and daily if the data is at least two cylces long. Other seasonality’s (monthly, quarterly) can be added manually. From the EDA of Apples stock price it was seen that, there are monthly and yearly stock price trends were seen. This will be interesting to note in the Seasonality analysis.

#### Modelling

Every seasonality’s can be represented by collection of frequency components (known as fourier\_order), which is important to determine for time-series modelling with seasonality. Here, we will run ranges of fourier\_order to find best possible RMSE values. For simplicity we will consider the fourier\_order for the month and quarter are the same.

A close up of a map

Description automatically generated

Best order for minimum RMSE score was found to be 5. With this the seasonality model will be trained and tested.

#### Plot the Forecasting

A close up of a map

Description automatically generated

Monthly, weekly, daywise and quarterly break down of the stock price from the modelling provide insights about the trend in the price.

#### Look Closely on the Test Data

A close up of a map

Description automatically generated

Adding seasonality included more randomness in the prediction and alignment with the test data.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_seasonality | 2063.07 | 35.23 | 45.42 | 0.20 | 535.98 |

Adding seasonality in the model improved the prediction score by more than 55 margins than the base model.

### Multiplicative Seasonality

By default, Phophet models forecast with seasonality and trend by additive method. It may not be always the case. Visually it is hard to tell from the time-series plot whether an additive or multiplicative model would be good fit. In this section we will explore how multiplicative seasonality perform over additive model.

#### Modelling

Like previous section, we will figure out the optimum Fourier components for multiplicative model.

A close up of a map

Description automatically generated

Best order for minimum RMSE score was found to be 25.

#### Look Closely on the Test Data

A close up of a map

Description automatically generated

Although there are series of spikes seen over the forecast line, the trend matches with the observation till the tail end.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_multiple\_seasonalities | 1838.21 | 34.55 | 42.87 | 0.22 | 478.96 |

Multiplicative model improved over additive model by a margin of 57 points in terms of average\_score.

### Holiday Effects

Holidays can have drastic effect on the stock price, trend. For example, stock seen historically slack time during Christmas, because people are busy buying in the shopping market other than the stock. FBProphet can include list of holidays over the train and test duration. The model pays special attention to these points and learns from the changing trend accordingly.

#### Modelling

in this section, we ran a function to determine the optimal effective days for which the RMSE error will be minimum. It would be best to get individual effective days for every types of holidays. For simplicity of analysis we will find a single effective day for all holidays.

A close up of a map

Description automatically generated

This shows, on average after 6 days of holidays the stock prediction gets its best

#### Look Closely on the Test Data

A close up of a map

Description automatically generated

Prediction follows the test data over most of the duration.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_holidays | 1761.25 | 31.33 | 41.96 | 0.17 | 458.68 |

Adding holidays improved the average\_score by a margin of 132 than the base model.

### Combined Model

Improvements were seen in terms of score and trend alignment when trend change option was tweaked, seasonality and holidays added in the models. Here we will come up with a single model with the combinations all these effects.

#### Modelling

Best parameters determined earlier for trend change scale, multiplicative seasonality Fourier order and holidays effect will be combined for this model. It was found that removing quarterly seasonality yield best possible model performances.

#### Look Closely on the Test Data

A close up of a map

Description automatically generated

Over the test data duration, predicted price showed better alignments with the observed price data.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_combined | 1450.45 | 31.41 | 38.08 | 0.20 | 380.04 |

Although the average\_score is not the best from the FBProphet models, this model includes important factors such as trend chage points, seasonalities (monthly, yearly) and holidays effect.

### Residual Modelling

The difference between observed and predicted model is called residue of a model. Generally the residuals are considered white noise (if modelled properly) and can not be modelled by any mathematical trend or seasonality components. There are many ways to model residual error with the main model. Here, we will utilise the 'add regressor' option of the FBProphet. The 'add regressor' puts extra weights while building the model. The weights are proportional to the regressor values added. As a regressor value we will add the residuals in our model, that is the difference between the observed values and the predicted values.

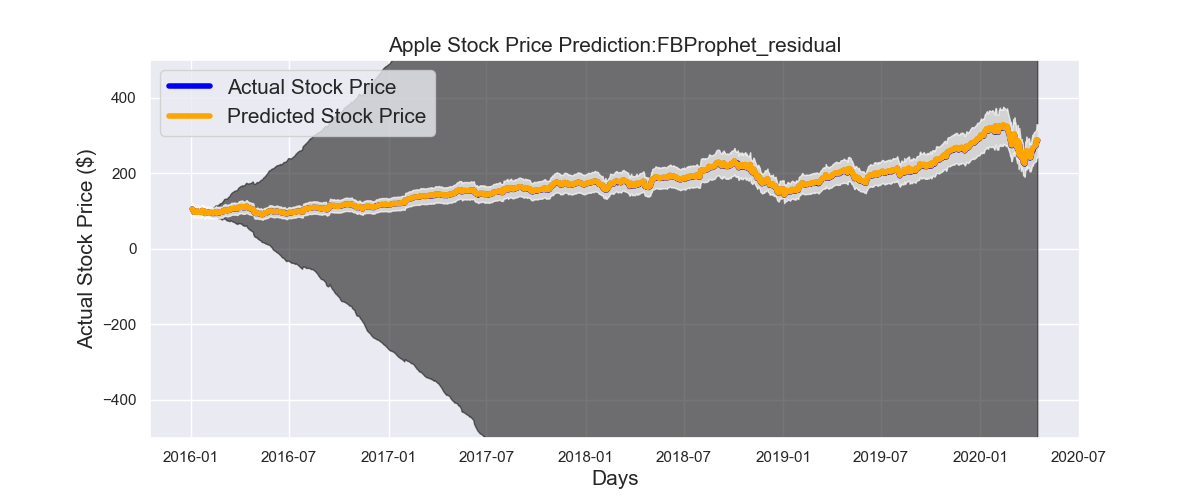
#### Plot the Forecasting

A close up of a map

Description automatically generated

Apparently heavy overlapping has been observed between observed and forecast data.

#### Look Closely on the Test Data



Visually the predicted values align very well with the observed data.

#### Model Performance Evaluation

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | mse | mae | rmse | mape | average\_score |
| FBProphet\_residual | 0.67 | 0.72 | 0.81 | 0.003 | 0.55 |

The average\_score is the lowest of all the models discussed so far.

## Model Evaluations

Now score data from all the models are available in terms of MSE, MAE, RMSE, MAPE and average\_score. We will display and compare results from the various modelling.

### Tabular Chart

Let us tabulate the performance score for the models we have discussed so far.

|  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- |
| model | MSE | MAE | RMSE | MAPE | AVERAGE\_SCORE |
| ARIMA | 2288.39 | 36.92 | 47.83 | 0.19 | 593.33 |
| FBProphet\_base | 2277.77 | 35.64 | 47.72 | 0.19 | 590.33 |
| FBProphet\_saturating | 20332.25 | 129.26 | 142.59 | 0.71 | 5151.20 |
| FBProphet\_trendchange | 1241.24 | 28.52 | 35.23 | 0.18 | 326.29 |
| FBProphet\_seasonality | 2063.07 | 35.23 | 45.42 | 0.20 | 535.98 |
| FBProphet\_multiple\_seasonalities | 1838.21 | 34.55 | 42.87 | 0.22 | 478.96 |
| FBProphet\_holidays | 1761.25 | 31.33 | 41.96 | 0.17 | 458.68 |
| FBProphet\_combined | 1450.45 | 31.41 | 38.08 | 0.21 | 380.04 |
| FBProphet\_residual | 0.67 | 0.72 | 0.81 | 0.003 | 0.55 |

We can see that, the FBProphet model will residual modelling yield best possible scores.

### Bar Plot

A screenshot of a cell phone

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In every measure FBprophet with residual effect tops the chart.

# Conclusion

The following is the summary of the analysis:

* Time-series closing price was taken from 1998-2020 to predict Apple's stock price
* This is a time-series forecasting problem and following models were applied:
  + ARIMA
  + FBPhophet
* Training data was split upto 2016 and the rest of the data was used for test data
* Hyperparameters of ARIMA model were optimized using grid search method. The best parameters were found to be (p, d, q = 0 , 1, 0)
* Four scoring measures were used: mean square error (MSE), mean absolute error (MAE), root mean square error (RMSE), mean absolute percentage error (MAEP). 'Average\_score' measure was introduced which takes average of all the metrics and provides a single number to represent the goodness of a model
* Average\_score for best ARIMA model is 593
* FBProphet's base model was trained for a reference and comparison as we add parameters (trend change, seasonality, hoidays) in the models. FBProphets base average score is 590.
* Adding trend change, seasonalities (yearly, monthly and quarterly) and holidays effects on forecasting seen improvements in terms of average scoring.
* Model with only adding trend change and yearly, monthly seasonality produced best metrics (325)
* Finally, a model that considered the effect of residuals as the difference between observed and forecasted, shown great promise in terms of all the performance metrics (average\_score =0.55).
* Couple of observations from the seasonality trend:
  + **day wise** : Stock price seen gradual increase from Monday to Friday in the forecast
  + **yearly** : Gradual increase of stock price forecast from January to June. July hit the lowest price of the year and then gradual increase till December
* ARIMA forecast line provided better alignment with observed price for initial one year. The line trajectory later on diverged with no seasonal components.
* Residual FBProphet model presented much better alignment with the observed price and captured well the seasonality, randomness of the price data for almost the four years.
* The residual model and prediction were saved for future use

# Future Directions

* Grid search technique can be deployed to know the best possible hyperparameters for FBProphet which is computationally expensive. This can be accomplished over cloud computation.
* App deployment can be done to predict for next couple of days or months stock data with confidence level.